

These are the *Mathematica* solutions for the paper:

“Permutation-type solutions to the Yang-Baxter and other n-simplex equations” by J. Hietarinta.

computations by Dara O Shayda

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<< Notation`

This formulation is incomprehensible and I guessed how it works:

In order to write the n -simplex equations in terms of A and B let us further define (in analogue with (2))

$$(A_{K_1 \dots K_n})_i^j = \begin{cases} A_\alpha^\beta, & \text{if } i = K_\alpha, j = K_\beta \text{ for some } \alpha, \beta, \\ \delta_i^j, & \text{otherwise,} \end{cases} \quad (11)$$

$$(B_{K_1 \dots K_n})_i = \begin{cases} B_i, & \text{if } i = K_\alpha, \text{ for some } \alpha, \\ 0, & \text{otherwise,} \end{cases} \quad (12)$$

so that

$$(R_{K_1 \dots K_n})_{i_1 \dots i_N}^{j_1 \dots j_N} = \prod_{\mu=1}^N \delta_{(A_{K_1 \dots K_n})_\mu^{i_\mu} + (B_{K_1 \dots K_n})_\mu}^{j_\mu}, \quad (13)$$

where now the ν summation runs from 1 to N .

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Notation[  $R_{i,j}$   $\Rightarrow$  makeA[A, {i_, j_}, 3] ]
Notation[  $R_{i,j,k}$   $\Rightarrow$  makeA[A, {i_, j_, k_}, 6] ]
Notation[  $R_{i,j,k,h}$   $\Rightarrow$  makeA[A, {i_, j_, k_, h_}, 10] ]

makeMatrix[dim_, a_] := Array[Subscript[a, #1, #2] &, dim]

(* makeA generates the A matrices in Hietarinta paper *)

makeA[A_, list_, n_] := Module[{res, i, j, k},

  res = ConstantArray[-1, {n, n}];

  Table[If[MemberQ[list, i] != True, res[[i]][[j]] = KroneckerDelta[i, j];
    res[[j]][[i]] = KroneckerDelta[j, i] ], {i, 1, n}, {j, 1, n}];

  Table[k = 1; Table[
    If[res[[list[[i]]]][[j]] == -1, res[[list[[i]]]][[j]] = A[[i]][[k]]; k = k + 1];,
    {j, 1, n}], {i, 1, Length[list]}];
  res

]

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4-simplex

In[30]:=

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A = makeMatrix[{4, 4}, a];
A // MatrixForm

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Out[31]//MatrixForm=

$$\begin{pmatrix} a_{1,1} & a_{1,2} & a_{1,3} & a_{1,4} \\ a_{2,1} & a_{2,2} & a_{2,3} & a_{2,4} \\ a_{3,1} & a_{3,2} & a_{3,3} & a_{3,4} \\ a_{4,1} & a_{4,2} & a_{4,3} & a_{4,4} \end{pmatrix}$$

Make the R matrices:

In[32]:= **R_{1,2,3,4} // MatrixForm**

Out[32]//MatrixForm=

$$\begin{pmatrix} a_{1,1} & a_{1,2} & a_{1,3} & a_{1,4} & 0 & 0 & 0 & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & a_{2,3} & a_{2,4} & 0 & 0 & 0 & 0 & 0 & 0 \\ a_{3,1} & a_{3,2} & a_{3,3} & a_{3,4} & 0 & 0 & 0 & 0 & 0 & 0 \\ a_{4,1} & a_{4,2} & a_{4,3} & a_{4,4} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

In[33]:= **R_{1,5,6,7} // MatrixForm**

Out[33]//MatrixForm=

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 & a_{1,2} & a_{1,3} & a_{1,4} & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ a_{2,1} & 0 & 0 & 0 & a_{2,2} & a_{2,3} & a_{2,4} & 0 & 0 & 0 \\ a_{3,1} & 0 & 0 & 0 & a_{3,2} & a_{3,3} & a_{3,4} & 0 & 0 & 0 \\ a_{4,1} & 0 & 0 & 0 & a_{4,2} & a_{4,3} & a_{4,4} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

In[34]:=

R_{2,5,8,9} // MatrixForm

Out[34]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & a_{1,1} & 0 & 0 & a_{1,2} & 0 & 0 & a_{1,3} & a_{1,4} & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & a_{2,1} & 0 & 0 & a_{2,2} & 0 & 0 & a_{2,3} & a_{2,4} & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & a_{3,1} & 0 & 0 & a_{3,2} & 0 & 0 & a_{3,3} & a_{3,4} & 0 \\ 0 & a_{4,1} & 0 & 0 & a_{4,2} & 0 & 0 & a_{4,3} & a_{4,4} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

In[35]:=

R_{3,6,8,10} // MatrixForm

Out[35]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_{1,1} & 0 & 0 & a_{1,2} & 0 & a_{1,3} & 0 & a_{1,4} \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_{2,1} & 0 & 0 & a_{2,2} & 0 & a_{2,3} & 0 & a_{2,4} \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & a_{3,1} & 0 & 0 & a_{3,2} & 0 & a_{3,3} & 0 & a_{3,4} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & a_{4,1} & 0 & 0 & a_{4,2} & 0 & a_{4,3} & 0 & a_{4,4} \end{pmatrix}$$

In[36]:=

R_{4,7,9,10} // MatrixForm

Out[36]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{1,1} & 0 & 0 & a_{1,2} & 0 & a_{1,3} & a_{1,4} \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{2,1} & 0 & 0 & a_{2,2} & 0 & a_{2,3} & a_{2,4} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{3,1} & 0 & 0 & a_{3,2} & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & a_{4,1} & 0 & 0 & a_{4,2} & 0 & a_{4,3} & a_{4,4} \end{pmatrix}$$

Too large set of equations of 3rd degree to printout:

In[37]:=

(R_{1,2,3,4} · R_{1,5,6,7} · R_{2,5,8,9} · R_{3,6,8,10} · R_{4,7,9,10} - R_{4,7,9,10} · R_{3,6,8,10} · R_{2,5,8,9} · R_{1,5,6,7} · R_{1,2,3,4}) //
MatrixForm

Out[37]//MatrixForm=

$$\begin{pmatrix} 0 \\ -a_{1,1} a_{1,2} a_{2,1} \\ -a_{1,3} a_{2,1} a_{3,1} - a_{1,1} (a_{1,2} a_{3,1} + a_{1,3} a_{2,1} a_{3,2}) \\ -a_{1,4} a_{3,1} a_{4,1} - a_{2,1} (a_{1,3} a_{4,1} + a_{1,4} a_{3,1} a_{4,3}) - a_{1,1} (a_{1,2} a_{4,1} + a_{1,4} a_{3,1} a_{4,2} + a_{2,1} (a_{1,3} a_{4,2,1} - a_{2,1}^2 - a_{1,1} a_{2,1} a_{2,2} \\ a_{3,1} - a_{2,1} a_{3,1} - a_{2,1} a_{2,3} a_{3,1} - a_{1,1} (a_{2,2} a_{3,1} + a_{2,1} a_{2,3} a_{3,2}) \\ a_{4,1} - a_{2,1} a_{4,1} - a_{2,4} a_{3,1} a_{4,1} - a_{2,1} (a_{2,3} a_{4,1} + a_{2,4} a_{3,1} a_{4,3}) - a_{1,1} (a_{2,2} a_{4,1} + a_{2,4} a_{3,1} a_{4,2} + a_{2,1} (\\ -a_{3,1}^2 - a_{2,1} a_{3,1} a_{3,3} - a_{1,1} (a_{3,1} a_{3,2} + a_{2,1} a_{3,2} a_{3,3}) \\ -a_{3,1} a_{4,1} - a_{3,1} a_{3,4} a_{4,1} - a_{2,1} (a_{3,3} a_{4,1} + a_{3,1} a_{3,4} a_{4,3}) - a_{1,1} (a_{3,2} a_{4,1} + a_{3,1} a_{3,4} a_{4,2} + a_{2,1} (a_{3,2} \\ -a_{4,1}^2 - a_{3,1} a_{4,1} a_{4,4} - a_{2,1} (a_{4,1} a_{4,3} + a_{3,1} a_{4,3} a_{4,4}) - a_{1,1} (a_{4,1} a_{4,2} + a_{3,1} a_{4,2} a_{4,4} + a_{2,1} (a_{4,2} \end{pmatrix}$$

In[38]:=

sol = Solve[
R_{1,2,3,4} · R_{1,5,6,7} · R_{2,5,8,9} · R_{3,6,8,10} · R_{4,7,9,10} - R_{4,7,9,10} · R_{3,6,8,10} · R_{2,5,8,9} · R_{1,5,6,7} · R_{1,2,3,4} ==
ConstantArray[0, {10, 10}], Flatten[A]];

In[39]:=

sol2 = DeleteDuplicates[sol];
Length[sol2]

Out[40]= 793

Note the variables for the solutions:

In[41]:=

Flatten[A]Out[41]= {a_{1,1}, a_{1,2}, a_{1,3}, a_{1,4}, a_{2,1}, a_{2,2}, a_{2,3}, a_{2,4}, a_{3,1}, a_{3,2}, a_{3,3}, a_{3,4}, a_{4,1}, a_{4,2}, a_{4,3}, a_{4,4}}

I see none of these solutions or even hint from Hietaina paper:

In[43]:=

Table[A /. sol2[[i]] // MatrixForm, {i, 1, Length[sol2]}]

$$\begin{aligned}
 & \left(\begin{array}{cccc} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ \frac{-a_{3,2}^2 + a_{3,1} a_{4,2} - a_{3,1} a_{3,2} a_{4,2} + a_{3,2}^2 a_{4,3}}{a_{3,2}^2 (-1 + a_{4,3})} & \frac{a_{4,2} - a_{3,2} a_{4,2}}{a_{3,2} (-1 + a_{4,3})} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,2} (-1 + a_{4,3})}{a_{4,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{array} \right), \\
 & \left(\begin{array}{cccc} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ \frac{-a_{3,1} a_{4,2} + a_{3,2} a_{4,3}}{a_{3,2} a_{4,3}} & -\frac{a_{4,2}}{a_{4,3}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{(-1 + a_{3,2}) a_{4,3}}{a_{4,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & a_{4,3} & \frac{a_{4,2} - a_{4,2} a_{4,3}}{(-1 + a_{3,2}) a_{4,3}} \end{array} \right), \\
 & \left(\begin{array}{cccc} \frac{a_{3,2} - a_{3,1} a_{4,2} - a_{3,2} a_{4,3}}{(-1 + a_{3,2}) a_{4,2}} & 0 & 0 & 0 \\ -\frac{a_{3,1} a_{4,2}}{a_{3,2} (-1 + a_{4,3})} & \frac{a_{4,2} - a_{3,2} a_{4,2}}{a_{3,2} (-1 + a_{4,3})} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,2} (-1 + a_{4,3})}{a_{4,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{array} \right), \\
 & \left(\begin{array}{cccc} \frac{a_{3,1} - a_{2,1} a_{3,1}}{a_{2,1} (-1 + a_{3,2})} & 0 & 0 & 0 \\ a_{2,1} & \frac{a_{2,1} (-1 + a_{3,2})}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & -\frac{a_{3,1}}{a_{2,1}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & \frac{a_{2,1} a_{3,2} - a_{3,1} a_{4,2}}{a_{2,1} a_{3,2}} & -\frac{a_{4,2}}{a_{3,2}} \end{array} \right), \left(\begin{array}{cccc} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1 + a_{2,1}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1} - a_{3,1} a_{3,2}}{(-1 + a_{2,1}) a_{3,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{array} \right), \\
 & \left(\begin{array}{cccc} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1 + a_{2,1}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1} - a_{3,1} a_{3,2}}{(-1 + a_{2,1}) a_{3,2}} & a_{3,4} \\ 0 & 0 & 0 & \frac{(-1 + a_{2,1}) a_{3,2} (-1 + a_{3,4})}{a_{3,1} (-1 + a_{3,2})} \end{array} \right), \left(\begin{array}{cccc} \frac{1 - a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1 - a_{3,4}}{a_{3,3}} \end{array} \right), \\
 & \left(\begin{array}{cccc} \frac{1 - a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{array} \right), \left(\begin{array}{cccc} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{array} \right), \left(\begin{array}{cccc} \frac{1 - a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1 - a_{3,4}}{a_{3,3}} \end{array} \right),
 \end{aligned}$$

$$\begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ a_{2,1} & \frac{1-a_{2,1}}{a_{1,1}} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & a_{1,2} & 0 & 0 \\ 0 & \frac{1-a_{1,2}}{a_{1,1}} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ a_{2,1} & \frac{1-a_{2,1}}{a_{1,1}} & 0 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & a_{1,2} & 0 & 0 \\ 0 & \frac{1-a_{1,2}}{a_{1,1}} & 0 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1}) a_{3,4}}{a_{2,4}} & 0 & 0 & 0 \\ a_{2,1} & -\frac{a_{2,4}}{a_{3,4}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{(-1+a_{2,3}) a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4}-a_{2,4} a_{3,4}}{(-1+a_{2,3}) a_{3,4}} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{a_{4,2}-a_{3,2} a_{4,2}}{a_{3,2} (-1+a_{4,3})} & 0 & 0 \\ 0 & a_{3,2} & \frac{a_{3,2} (-1+a_{4,3})}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & -\frac{a_{4,2}}{a_{4,3}} & 0 & 0 \\ 0 & a_{3,2} & \frac{(-1+a_{3,2}) a_{4,3}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & \frac{a_{4,2}-a_{4,2} a_{4,3}}{(-1+a_{3,2}) a_{4,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{3,2} (-1+a_{4,3})}{(-1+a_{3,2}) a_{4,2}} & a_{1,2} & 0 & 0 \\ 0 & \frac{a_{4,2}-a_{3,2} a_{4,2}}{a_{3,2} (-1+a_{4,3})} & 0 & 0 \\ 0 & a_{3,2} & \frac{a_{3,2} (-1+a_{4,3})}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{a_{3,1}-a_{2,1} a_{3,1}}{a_{2,1} (-1+a_{3,2})} & 0 & 0 & 0 \\ a_{2,1} & \frac{a_{2,1} (-1+a_{3,2})}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & -\frac{a_{3,1}}{a_{2,1}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,1} (-1+a_{3,4})}{a_{3,1}} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1+a_{2,1}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1}-a_{3,1} a_{3,2}}{(-1+a_{2,1}) a_{3,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & \frac{-a_{3,2}^2+a_{2,1} a_{3,2}^2+a_{3,1} a_{4,2}-a_{3,1} a_{3,2} a_{4,2}}{(-1+a_{2,1}) a_{3,2}^2} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{3,1}-a_{2,1} a_{3,1}}{a_{2,1} (-1+a_{3,2})} & 0 & 0 & 0 \\ a_{2,1} & \frac{a_{2,1} (-1+a_{3,2})}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & -\frac{a_{3,1}}{a_{2,1}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & a_{3,2} & \frac{1-a_{3,2}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{4,3}}{a_{4,2}} & a_{1,2} & 0 & 0 \\ 0 & -\frac{a_{4,2}}{a_{4,3}} & 0 & 0 \\ 0 & a_{3,2} & \frac{(-1+a_{3,2}) a_{4,3}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & \frac{a_{4,2}-a_{4,2} a_{4,3}}{(-1+a_{3,2}) a_{4,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & a_{3,2} & \frac{1-a_{3,2}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{1,3}-a_{1,2} a_{1,3}}{a_{1,2} (-1+a_{2,3})} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{a_{1,2} (-1+a_{2,3})}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{(-1+a_{1,2}) a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}-a_{1,3} a_{2,3}}{(-1+a_{1,2}) a_{2,3}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1}) a_{3,3}}{-1+a_{2,3}} & 0 & 0 & 0 \\ a_{2,1} & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1}) a_{2,3} (-1+a_{3,4})}{(-1+a_{2,3}) a_{2,4}} & 0 & 0 & 0 \\ a_{2,1} & \frac{a_{2,4}-a_{2,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3} (-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{3,3}}{-1+a_{3,2}} & a_{1,2} & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{1,3}-a_{1,2} a_{1,3}}{a_{1,2} (-1+a_{2,3})} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{a_{1,2} (-1+a_{2,3})}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 0 \\ 0 & 0 & a_{4,3} & \frac{a_{1,2} (-1+a_{4,3})}{a_{1,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & -\frac{a_{2,4}}{a_{3,4}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{(-1+a_{2,3}) a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4}-a_{2,4} a_{3,4}}{(-1+a_{2,3}) a_{3,4}} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{a_{2,4}-a_{2,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3} (-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{(-1+a_{1,2}) a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}-a_{1,3} a_{2,3}}{(-1+a_{1,2}) a_{2,3}} & 0 \\ 0 & 0 & a_{4,3} & \frac{(-1+a_{1,2}) a_{2,3} (-1+a_{4,3})}{a_{1,3} (-1+a_{2,3})} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & \frac{-a_{1,3} a_{2,4}+a_{2,3} a_{3,4}}{a_{2,3} a_{3,4}} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & -\frac{a_{2,4}}{a_{3,4}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{(-1+a_{2,3}) a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4}-a_{2,4} a_{3,4}}{(-1+a_{2,3}) a_{3,4}} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & \frac{-a_{2,3}^2+a_{1,3} a_{2,4}-a_{1,3} a_{2,3} a_{2,4}+a_{2,3}^2 a_{3,4}}{a_{2,3}^2 (-1+a_{3,4})} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & \frac{a_{2,4}-a_{2,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3} (-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{1,3}-a_{1,2} a_{1,3}}{a_{1,2} (-1+a_{2,3})} & a_{1,2} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & \frac{a_{1,2} (-1+a_{2,3})}{a_{1,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & \frac{a_{1,2} a_{2,3}-a_{1,3} a_{2,4}}{a_{1,2} a_{2,3}} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{2,3}-a_{1,3} a_{2,4}-a_{2,3} a_{3,4}}{(-1+a_{2,3}) a_{2,4}} & -\frac{a_{1,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & \frac{a_{2,4}-a_{2,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3} (-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{1,2} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & \frac{(-1+a_{1,2}) a_{2,3}}{a_{1,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{1,3}-a_{1,3} a_{2,3}}{(-1+a_{1,2}) a_{2,3}} & \frac{-a_{2,3}^2+a_{1,2} a_{2,3}^2+a_{1,3} a_{2,4}-a_{1,3} a_{2,3} a_{2,4}}{(-1+a_{1,2}) a_{2,3}^2} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1-a_{3,1} a_{4,2} & -a_{4,2} & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ a_{3,1} a_{4,2} & a_{4,2} & 1 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ a_{2,1} & \frac{-1+a_{2,1}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ a_{3,1} a_{4,2} & a_{4,2} & 1 & -a_{4,2} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ \frac{a_{3,2}^2-a_{3,1} a_{4,2}+a_{3,1} a_{3,2} a_{4,2}}{a_{3,2}^2} & \frac{(-1+a_{3,2}) a_{4,2}}{a_{3,2}} & 0 & 0 \\ a_{3,1} & a_{3,2} & -\frac{a_{3,2}}{a_{4,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & 0 & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ 0 & -\frac{a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1} (-1+a_{3,2})}{a_{3,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & \frac{a_{3,1} a_{4,2}}{a_{3,2}} & \frac{a_{3,2}-a_{3,1} a_{4,2}}{a_{3,1} (-1+a_{3,2})} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ 0 & -\frac{a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1} (-1+a_{3,2})}{a_{3,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & \frac{a_{3,2}^2-a_{3,1} a_{4,2}+a_{3,1} a_{3,2} a_{4,2}}{a_{3,2}^2} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ 0 & -\frac{a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1} (-1+a_{3,2})}{a_{3,2}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{3,2}-a_{3,2} a_{3,4}}{a_{3,1} (-1+a_{3,2})} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1+a_{2,1}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1}-a_{3,1} a_{3,2}}{(-1+a_{2,1}) a_{3,2}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1+a_{2,1}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1}-a_{3,1} a_{3,2}}{(-1+a_{2,1}) a_{3,2}} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} \frac{a_{3,2}-a_{3,1} a_{4,2}}{(-1+a_{3,2}) a_{4,2}} & 0 & 0 & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & \frac{(-1+a_{3,2}) a_{4,2}}{a_{3,2}} & 0 & 0 \\ a_{3,1} & a_{3,2} & -\frac{a_{3,2}}{a_{4,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & 0 & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & -\frac{a_{4,2}}{a_{4,3}} & 0 & 0 \\ 0 & a_{3,2} & \frac{(-1+a_{3,2}) a_{4,3}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & \frac{a_{4,2}-a_{4,2} a_{4,3}}{(-1+a_{3,2}) a_{4,3}} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1}) a_{4,3}}{a_{4,2}} & 0 & 0 & 0 \\ a_{2,1} & -\frac{a_{4,2}}{a_{4,3}} & 0 & 0 \\ 0 & 0 & -\frac{a_{4,3}}{a_{4,2}} & 0 \\ a_{4,3}-a_{2,1} a_{4,3} & a_{4,2} & a_{4,3} & \frac{a_{4,2}(-1+a_{4,3})}{a_{4,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{4,3}}{a_{4,2}} & a_{1,2} & 0 & 0 \\ 0 & -\frac{a_{4,2}}{a_{4,3}} & 0 & 0 \\ 0 & 0 & -\frac{a_{4,3}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & \frac{a_{4,2}(-1+a_{4,3})}{a_{4,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & -a_{3,1} & 0 \\ a_{3,1} a_{4,2} & a_{4,2} & 1-a_{3,1} a_{4,2} & -a_{4,2} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{3,2}-a_{3,2}^2-a_{3,1} a_{4,2}}{(-1+a_{3,2}) a_{4,2}} & 0 & 0 & 0 \\ -\frac{a_{3,1} a_{4,2}}{(-1+a_{3,2}) a_{3,2}} & -\frac{a_{4,2}}{a_{3,2}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{(-1+a_{3,2}) a_{3,2}}{a_{4,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & a_{3,2} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{3,2} & \frac{(-1+a_{3,2}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & -\frac{a_{3,1}}{a_{3,2}} & 0 \\ \frac{a_{3,1} a_{4,2}}{a_{3,2}} & a_{4,2} & -\frac{a_{3,1} a_{4,2}}{(-1+a_{3,2}) a_{3,2}} & \frac{a_{3,2}-a_{3,2}^2-a_{3,1} a_{4,2}}{a_{3,1}(-1+a_{3,2})} \end{pmatrix},$$

$$\begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ a_{2,1} & \frac{-1+a_{2,1}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1+a_{2,1}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1}-a_{3,1} a_{3,2}}{(-1+a_{2,1}) a_{3,2}} & 0 \\ 0 & 0 & 0 & \frac{a_{3,2}-a_{2,1} a_{3,2}}{a_{3,1}(-1+a_{3,2})} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{2,1}) a_{3,1}}{a_{2,1}} & 0 & 0 & 0 \\ a_{2,1} & -\frac{a_{2,1}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 0 & -\frac{a_{3,1}}{a_{2,1}} & 0 \\ a_{2,1} - a_{2,1} a_{4,3} & 0 & a_{4,3} & \frac{a_{2,1} (-1+a_{4,3})}{a_{3,1}} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1}) a_{3,1}}{a_{2,1}} & 0 & 0 & 0 \\ a_{2,1} & -\frac{a_{2,1}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 0 & -\frac{a_{3,1}}{a_{2,1}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & -\frac{a_{2,4}}{a_{3,4}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{(-1+a_{2,3}) a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4} - a_{2,4} a_{3,4}}{(-1+a_{2,3}) a_{3,4}} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,4}}{a_{2,4}} & 0 & 0 & 0 \\ 0 & -\frac{a_{2,4}}{a_{3,4}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{(-1+a_{2,3}) a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4} - a_{2,4} a_{3,4}}{(-1+a_{2,3}) a_{3,4}} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & \frac{a_{2,4} - a_{2,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3} (-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & -\frac{a_{2,4}}{a_{3,4}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{(-1+a_{2,3}) a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4} - a_{2,4} a_{3,4}}{(-1+a_{2,3}) a_{3,4}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{2,3} - a_{2,1} a_{2,3}}{(-1+a_{2,3}) a_{2,4}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1+a_{2,3}) a_{2,4}}{a_{2,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & -\frac{a_{2,3}}{a_{2,4}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & \frac{a_{2,4} - a_{2,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3} (-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{2,1}) a_{3,4}}{a_{2,4}} & 0 & 0 & 0 \\ a_{2,1} & -\frac{a_{2,4}}{a_{3,4}} & 0 & a_{2,4} \\ 0 & 0 & -\frac{a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4} (-1+a_{3,4})}{a_{3,4}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & -\frac{a_{2,4}}{a_{3,4}} & 0 & a_{2,4} \\ 0 & 0 & -\frac{a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4} (-1+a_{3,4})}{a_{3,4}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{3,4}}{a_{2,4}} & a_{1,2} & 0 & a_{3,4} - a_{1,2} a_{3,4} \\ 0 & -\frac{a_{2,4}}{a_{3,4}} & 0 & a_{2,4} \\ 0 & 0 & -\frac{a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,4} (-1+a_{3,4})}{a_{3,4}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & -a_{4,2} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & -a_{4,2} \end{pmatrix},$$

$$\begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & -a_{4,2} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \frac{a_{4,2}-a_{3,2} a_{4,2}}{a_{3,2} (-1+a_{4,3})} & 0 & 0 \\ 0 & a_{3,2} & \frac{a_{3,2} (-1+a_{4,3})}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}, \begin{pmatrix} \frac{a_{3,2}-a_{3,2} a_{4,3}}{(-1+a_{3,2}) a_{4,2}} & 0 & 0 & 0 \\ 0 & \frac{a_{4,2}-a_{3,2} a_{4,2}}{a_{3,2} (-1+a_{4,3})} & 0 & 0 \\ 0 & a_{3,2} & \frac{a_{3,2} (-1+a_{4,3})}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{(-1+a_{3,2}) a_{4,2}}{a_{3,2}} & 0 & 0 \\ 0 & a_{3,2} & -\frac{a_{3,2}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & 0 & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}, \begin{pmatrix} \frac{a_{3,2} - a_{1,2} a_{3,2}}{(-1+a_{3,2}) a_{4,2}} & a_{1,2} & 0 & 0 \\ 0 & \frac{(-1+a_{3,2}) a_{4,2}}{a_{3,2}} & 0 & 0 \\ 0 & a_{3,2} & -\frac{a_{3,2}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & 0 & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}$$

$$\begin{pmatrix} \mathbf{a}_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & \frac{-1+\mathbf{a}_{4,3}}{\mathbf{a}_{4,2}} & 0 \\ 0 & \mathbf{a}_{4,2} & \mathbf{a}_{4,3} & -\mathbf{a}_{4,2} \end{pmatrix}, \begin{pmatrix} \mathbf{a}_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & \frac{-1+\mathbf{a}_{4,3}}{\mathbf{a}_{4,2}} & 0 \\ 0 & \mathbf{a}_{4,2} & \mathbf{a}_{4,3} & -\mathbf{a}_{4,2} \end{pmatrix}, \begin{pmatrix} \mathbf{a}_{1,1} & 0 & 0 & 0 \\ 0 & -\mathbf{a}_{4,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & \mathbf{a}_{4,2} & 1 & \mathbf{a}_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2})}{-1+a_{3,2}} a_{3,3} & a_{1,2} & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{1,2})}{-1+a_{3,2}} a_{3,3} & a_{1,2} & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1}{a_{3,3}} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{3,3} - a_{1,2} a_{3,3} & a_{1,2} & 0 & 0 \\ 0 & \frac{1}{a_{3,3}} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix},$$

$$\begin{pmatrix} \mathbf{a}_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1}{\mathbf{a}_{3,3}} & 0 & 0 \\ 0 & 0 & \mathbf{a}_{3,3} & \mathbf{a}_{3,4} \\ 0 & 0 & 0 & \frac{1-\mathbf{a}_{3,4}}{\mathbf{a}_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{1}{\mathbf{a}_{2,2}} & 0 & 0 & 0 \\ 0 & \mathbf{a}_{2,2} & 0 & 0 \\ 0 & 0 & \mathbf{a}_{3,3} & \mathbf{a}_{3,4} \\ 0 & 0 & 0 & \frac{1-\mathbf{a}_{3,4}}{\mathbf{a}_{3,3}} \end{pmatrix}, \begin{pmatrix} \mathbf{a}_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1}{\mathbf{a}_{3,3}} & 0 & 0 \\ 0 & 0 & \mathbf{a}_{3,3} & 0 \\ 0 & 0 & 0 & \mathbf{a}_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{3,3} - a_{1,2} a_{3,3} & a_{1,2} & 0 & 0 \\ 0 & \frac{1}{a_{3,3}} & 0 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \\
\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1}) a_{3,1}}{a_{2,1}} & 0 & 0 & 0 \\ a_{2,1} & -\frac{a_{2,1}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 0 & -\frac{a_{3,1}}{a_{2,1}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{2,1}(-1+a_{3,4})}{a_{3,1}} \end{pmatrix}, \\
\begin{pmatrix} \frac{a_{3,1}-a_{2,1} a_{3,1}}{a_{2,1}(-1+a_{3,2})} & 0 & 0 & 0 \\ a_{2,1} & \frac{a_{2,1}(-1+a_{3,2})}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & -\frac{a_{3,1}}{a_{2,1}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \\
\begin{pmatrix} -a_{1,3} & a_{1,2} & a_{1,3} & a_{1,3} a_{2,4} \\ 0 & \frac{-1+a_{1,2}}{a_{1,3}} & 1 & a_{2,4} \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & a_{1,3} a_{2,4} \\ 0 & 0 & 1 & a_{2,4} \\ 0 & 0 & \frac{-1+a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & \frac{-1+a_{4,3}}{a_{4,2}} & 0 \\ a_{3,1} a_{4,2} & a_{4,2} & a_{4,3} & -a_{4,2} \end{pmatrix}, \\
\begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & \frac{a_{4,2}-a_{3,2} a_{4,2}}{a_{3,2}(-1+a_{4,3})} & 0 & 0 \\ 0 & a_{3,2} & \frac{a_{3,2}(-1+a_{4,3})}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & \frac{a_{4,2}-a_{3,2} a_{4,2}}{a_{3,2}(-1+a_{4,3})} & 0 & 0 \\ 0 & a_{3,2} & \frac{a_{3,2}(-1+a_{4,3})}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & -\frac{a_{4,2}}{a_{3,2}} \end{pmatrix}, \\
\begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & a_{3,2} & \frac{1-a_{3,2}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \\
\begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & -a_{3,1} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ a_{2,1} & \frac{(-1+a_{2,1}) a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1}-a_{3,1} a_{3,2}}{(-1+a_{2,1}) a_{3,2}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},
\end{pmatrix}$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{-1+a_{1,2}}{a_{4,2}} & a_{1,2} & 0 & 0 \\ 0 & -a_{4,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{4,3}}{a_{4,2}} & 0 & 0 & 0 \\ 0 & -\frac{a_{4,2}}{a_{4,3}} & 0 & 0 \\ 0 & a_{3,2} & \frac{(-1+a_{3,2}) a_{4,3}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & \frac{a_{4,2}-a_{4,2} a_{4,3}}{(-1+a_{3,2}) a_{4,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & a_{3,2} & \frac{1-a_{3,2}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & a_{3,2} & \frac{1-a_{3,2}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,2}}{-1+a_{3,2}} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{-1+a_{1,2}}{a_{1,3}} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{(-1+a_{1,2}) a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}-a_{1,3} a_{2,3}}{(-1+a_{1,2}) a_{2,3}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{1,3}}{a_{1,2}} & a_{1,2} & a_{1,3} & 0 \\ 0 & -\frac{a_{1,2}}{a_{1,3}} & 0 & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -a_{1,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & 0 & a_{1,3} & 0 \\ 0 & -\frac{a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}(-1+a_{2,3})}{a_{2,3}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{(-1+a_{1,2}) a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}-a_{1,3} a_{2,3}}{(-1+a_{1,2}) a_{2,3}} & 0 \\ 0 & 0 & 0 & \frac{a_{2,3}-a_{1,2} a_{2,3}}{a_{1,3}(-1+a_{2,3})} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -a_{1,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{-1+a_{4,3}}{a_{1,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{1,3}-a_{1,2} a_{1,3}}{a_{1,2}(-1+a_{2,3})} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{a_{1,2}(-1+a_{2,3})}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 0 \\ 0 & 0 & 0 & -\frac{a_{1,2}}{a_{1,3}} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{(-1+a_{1,2}) a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}-a_{1,3} a_{2,3}}{(-1+a_{1,2}) a_{2,3}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \frac{a_{2,4}-a_{2,3}a_{2,4}}{a_{2,3}(-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3}(-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{(-1+a_{2,3})a_{2,4}}{a_{2,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & -\frac{a_{2,3}}{a_{2,4}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \\
\begin{pmatrix} -\frac{a_{3,3}}{-1+a_{3,2}} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{1,2})a_{3,3}}{-1+a_{3,2}} & a_{1,2} & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{1,2})a_{3,3}}{-1+a_{3,2}} & a_{1,2} & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \\
\begin{pmatrix} a_{3,3}-a_{1,2}a_{3,3} & a_{1,2} & 0 & 0 \\ 0 & \frac{1}{a_{3,3}} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{4,4} \end{pmatrix}, \\
\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{-1+a_{1,2}}{a_{1,3}} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{4,4} \end{pmatrix}, \\
\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & 0 & a_{1,3} & 0 \\ 0 & -\frac{a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}(-1+a_{2,3})}{a_{2,3}} & 0 \\ 0 & 0 & a_{4,3} & \frac{a_{2,3}-a_{2,3}a_{4,3}}{a_{1,3}(-1+a_{2,3})} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{1,2})a_{1,3}}{a_{1,2}} & a_{1,2} & a_{1,3} & 0 \\ 0 & -\frac{a_{1,2}}{a_{1,3}} & 0 & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 0 \\ 0 & 0 & a_{4,3} & \frac{a_{1,2}(-1+a_{4,3})}{a_{1,3}} \end{pmatrix}, \\
\begin{pmatrix} -a_{1,3} & 1-a_{1,3}a_{2,4} & a_{1,3} & a_{1,3}a_{2,4} \\ 0 & -a_{2,4} & 1 & a_{2,4} \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,3}}{-1+a_{3,2}} & 0 & 0 & 0 \\ 0 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \\
\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} a_{3,3}-a_{2,1}a_{3,3} & 0 & 0 & 0 \\ a_{2,1} & \frac{1}{a_{3,3}} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1})a_{3,3}}{-1+a_{2,3}} & 0 & 0 & 0 \\ a_{2,1} & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},
\end{pmatrix}$$

$$\begin{pmatrix} \frac{a_{2,3}-a_{2,3} a_{3,4}}{(-1+a_{2,3}) a_{2,4}} & 0 & 0 & 0 \\ 0 & \frac{a_{2,4}-a_{2,3} a_{2,4}}{a_{2,3} (-1+a_{3,4})} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{2,3} (-1+a_{3,4})}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & a_{1,3} & a_{1,3} a_{2,4} \\ 0 & 0 & 1 & a_{2,4} \\ 0 & 0 & -a_{1,3} & 1-a_{1,3} a_{2,4} \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{1,3}}{a_{1,2}} & a_{1,2} & a_{1,3} & a_{1,2}-a_{1,2} a_{3,4} \\ 0 & -\frac{a_{1,2}}{a_{1,3}} & 0 & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & a_{3,4} \\ 0 & 0 & 0 & \frac{a_{1,2} (-1+a_{3,4})}{a_{1,3}} \end{pmatrix}, \begin{pmatrix} \frac{a_{1,3}-a_{1,2} a_{1,3}}{a_{1,2} (-1+a_{2,3})} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{a_{1,2} (-1+a_{2,3})}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{1,3}-a_{1,2} a_{1,3}}{a_{1,2} (-1+a_{2,3})} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{a_{1,2} (-1+a_{2,3})}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} \frac{a_{1,3}-a_{1,2} a_{1,3}}{a_{1,2} (-1+a_{2,3})} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{a_{1,2} (-1+a_{2,3})}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{(-1+a_{1,2}) a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}-a_{1,3} a_{2,3}}{(-1+a_{1,2}) a_{2,3}} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & \frac{a_{2,3}^2-a_{1,3} a_{2,4}+a_{1,3} a_{2,3} a_{2,4}}{a_{2,3}^2} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & \frac{(-1+a_{2,3}) a_{2,4}}{a_{2,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & -\frac{a_{2,3}}{a_{2,4}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} \frac{a_{2,3}-a_{2,3}^2-a_{1,3} a_{2,4}}{(-1+a_{2,3}) a_{2,4}} - \frac{a_{1,3} a_{2,4}}{(-1+a_{2,3}) a_{2,3}} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & -\frac{a_{2,4}}{a_{2,3}} & a_{2,4} \\ 0 & 0 & \frac{(-1+a_{2,3}) a_{2,3}}{a_{2,4}} & a_{2,3} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & 0 & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & -\frac{a_{2,3}}{a_{1,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{1,3} (-1+a_{2,3})}{a_{2,3}} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & 0 & 0 & \frac{a_{2,3}-a_{1,3} a_{2,4}}{a_{1,3} (-1+a_{2,3})} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & a_{2,3} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & \frac{(-1+a_{2,3}) a_{2,3}}{a_{1,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & -\frac{a_{1,3}}{a_{2,3}} & -\frac{a_{1,3} a_{2,4}}{(-1+a_{2,3}) a_{2,3}} \\ 0 & 0 & 0 & \frac{a_{2,3}-a_{2,3}^2-a_{1,3} a_{2,4}}{a_{1,3} (-1+a_{2,3})} \end{pmatrix}, \begin{pmatrix} \frac{a_{2,3}-a_{1,3} a_{2,4}}{(-1+a_{2,3}) a_{2,4}} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & \frac{(-1+a_{2,3}) a_{2,4}}{a_{2,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & -\frac{a_{2,3}}{a_{2,4}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & 0 & a_{1,3} & \frac{a_{1,3} a_{2,4}}{a_{2,3}} \\ 0 & -\frac{a_{2,3}}{a_{1,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{a_{1,3} (-1+a_{2,3})}{a_{2,3}} & \frac{a_{2,3}^2 - a_{1,3} a_{2,4} + a_{1,3} a_{2,3} a_{2,4}}{a_{2,3}^2} \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & \frac{1}{a_{2,2}} & 0 \\ 0 & 0 & a_{4,3} & a_{2,2} - a_{2,2} a_{4,3} \end{pmatrix}, \\
\begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & \frac{1}{a_{2,2}} & 0 \\ 0 & 0 & a_{4,3} & a_{2,2} - a_{2,2} a_{4,3} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & a_{4,3} & \frac{a_{2,2} (-1+a_{4,3})}{-1+a_{2,3}} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & a_{4,3} & \frac{a_{2,2} (-1+a_{4,3})}{-1+a_{2,3}} \end{pmatrix}, \\
\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{2,4} \\ 0 & 0 & \frac{-1+a_{3,4}}{a_{2,4}} & a_{3,4} \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} \frac{(-1+a_{2,1}) a_{3,3}}{-1+a_{2,3}} & 0 & 0 & 0 \\ a_{2,1} & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 - a_{3,1} a_{4,2} & -a_{4,2} & 0 & 0 \\ a_{3,1} & 1 & 0 & 1 \\ a_{3,1} a_{4,2} & a_{4,2} & 1 & 0 \end{pmatrix}, \\
\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 0 & -\frac{1}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ a_{3,1} a_{4,2} & a_{4,2} & 1 & -a_{4,2} \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ a_{3,1} a_{4,2} & a_{4,2} & 1 & -a_{4,2} \end{pmatrix}, \begin{pmatrix} \frac{2 a_{3,1}}{a_{3,1} a_{4,2} + \sqrt{a_{3,1}} \sqrt{a_{4,2}} \sqrt{4+a_{3,1} a_{4,2}}} \\ 0 \\ a_{3,1} \\ \frac{2 a_{3,1} a_{4,2}}{-a_{3,1} a_{4,2} - \sqrt{a_{3,1}} \sqrt{a_{4,2}} \sqrt{4+a_{3,1} a_{4,2}}} \end{pmatrix}, \frac{2}{-a_{3,1} a_{4,2} - \sqrt{a_{3,1}} \sqrt{a_{4,2}} \sqrt{4+a_{3,1} a_{4,2}}} \left(-a_{3,1} i \right. \\
\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ a_{2,1} & \frac{-1+a_{2,1}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 0 & -\frac{1}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & a_{3,3} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ a_{2,1} & \frac{-1+a_{2,1}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \\
\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ 0 & -\frac{a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1} (-1+a_{3,2})}{a_{3,2}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ 0 & -\frac{a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1} (-1+a_{3,2})}{a_{3,2}} & 0 \\ 0 & 0 & 0 & \frac{a_{3,2}}{a_{3,1} (-1+a_{3,2})} \end{pmatrix},
\end{pmatrix}$$

$$\left(\begin{array}{cccc} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{array} \right), \quad \left(\begin{array}{c} \frac{2 a_{3,1}}{a_{3,1} a_{4,2} + \sqrt{a_{3,1}} \sqrt{a_{4,2}} \sqrt{4 + a_{3,1} a_{4,2}}} \\ 0 \\ a_{3,1} \\ \frac{2 a_{3,1} a_{4,2}}{-a_{3,1} a_{4,2} - \sqrt{a_{3,1}} \sqrt{a_{4,2}} \sqrt{4 + a_{3,1} a_{4,2}}} \end{array} \right), \quad \left(\begin{array}{c} 0 \\ \frac{2 + a_{3,1} a_{4,2} + \sqrt{a_{3,1}} \sqrt{a_{4,2}} \sqrt{4 + a_{3,1} a_{4,2}}}{a_{3,1} + \frac{\sqrt{a_{3,1}} \sqrt{4 + a_{3,1} a_{4,2}}}{\sqrt{a_{4,2}}}} \\ \frac{1}{2} \left(-a_{3,1} a_{4,2} - \sqrt{a_{3,1}} \sqrt{a_{4,2}} \sqrt{4 + a_{3,1} a_{4,2}} \right) \\ a_{4,2} \end{array} \right)$$

$$\begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 0 & \frac{1}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{2,2} \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & \frac{1}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{2,2} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ 0 & 0 & 1 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,2}}{-1+a_{2,3}} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & a_{2,2} & a_{2,3} & 0 \\ 0 & 0 & \frac{1-a_{2,3}}{a_{2,2}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & \frac{1}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

[illegible]

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & a_{3,4} \\ 0 & 0 & 0 & \frac{1-a_{3,4}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & a_{4,3} & \frac{1-a_{4,3}}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & -a_{3,1} & a_{3,4} \\ 0 & 0 & 0 & \frac{-1+a_{3,4}}{a_{3,1}} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & -a_{3,1} & 0 \\ -a_{4,3} & 0 & a_{4,3} & \frac{-1+a_{4,3}}{a_{3,1}} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & -a_{3,1} & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,1}}{a_{3,2}} & 0 & 0 & 0 \\ 0 & -\frac{a_{3,2}}{a_{3,1}} & 0 & 0 \\ a_{3,1} & a_{3,2} & \frac{a_{3,1}(-1+a_{3,2})}{a_{3,2}} & 0 \\ -\frac{a_{3,2}}{-1+a_{3,2}} & -\frac{a_{3,2}^2}{a_{3,1}(-1+a_{3,2})} & 0 & \frac{a_{3,2}}{a_{3,1}(-1+a_{3,2})} \end{pmatrix},$$

$$\begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{1}{a_{4,2}} & 0 & 0 & 0 \\ 0 & -a_{4,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & a_{4,4} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & -a_{4,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{-1+a_{2,1}}{a_{4,2}} & 0 & 0 & 0 \\ a_{2,1} & -a_{4,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & -a_{4,2} \end{pmatrix},$$

$$\begin{pmatrix} \frac{1-a_{1,2}}{a_{2,2}} & a_{1,2} & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} \frac{1-a_{2,1}}{a_{2,2}} & 0 & 0 & 0 \\ a_{2,1} & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & a_{3,2} & \frac{1-a_{3,2}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & a_{3,2} & \frac{1-a_{3,2}}{a_{2,2}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,2}}{-1+a_{3,2}} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -a_{1,3} & a_{1,2} & a_{1,3} & 0 \\ 0 & \frac{-1+a_{1,2}}{a_{1,3}} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} -a_{1,3} & 0 & a_{1,3} & 0 \\ 0 & -\frac{1}{a_{1,3}} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & \frac{1}{a_{3,3}} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & 0 & a_{1,3} & 0 \\ 0 & -\frac{a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}(-1+a_{2,3})}{a_{2,3}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

[illegible]

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 1 \\ 0 & a_2 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{1}{a_{2,4}} & 0 & 0 & 0 \\ 0 & -a_{2,4} & a_{2,3} & a_{2,4} \\ 0 & 0 & \frac{-1+a_{2,3}}{a_{2,4}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\left(\begin{array}{cccc} \frac{a_{2,3}}{(-1+a_{2,3}) a_{2,4}} & 0 & 0 & 0 \\ 0 & \frac{(-1+a_{2,3}) a_{2,4}}{a_{2,3}} & a_{2,3} & a_{2,4} \\ 0 & 0 & -\frac{a_{2,3}}{a_{2,4}} & 0 \\ 0 & 0 & 0 & -\frac{a_{2,4}}{a_{2,3}} \end{array} \right), \left(\begin{array}{ccc} \frac{a_{2,3}}{(-1+a_{2,3}) a_{2,4}} & 0 & -\frac{a_{2,3}^2}{(-1+a_{2,3}) a_{2,4}} - \frac{a_{2,3}}{-1+a_{2,3}} \\ 0 & \frac{(-1+a_{2,3}) a_{2,4}}{a_{2,3}} & a_{2,3} a_{2,4} \\ 0 & 0 & -\frac{a_{2,3}}{a_{2,4}} 0 \\ 0 & 0 & 0 -\frac{a_{2,4}}{a_{2,3}} \end{array} \right),$$

$$\begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 0 & a_{1,3} & 1 \\ 0 & -\frac{1}{a_{1,3}} & 1 & \frac{1}{a_{1,3}} \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & -a_{4,2} \end{pmatrix},$$

$$\begin{pmatrix} -a_{1,3} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & a_{4,2} & 1 & -a_{4,2} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} -a_{1,3} & 0 & a_{1,3} & 0 \\ 0 & -\frac{1}{a_{1,3}} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2})}{a_{1,2}} a_{1,2} & a_{1,2} & a_{1,3} & 0 \\ 0 & -\frac{a_{1,2}}{a_{1,3}} & 0 & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{2,4} \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 1 & a_{2,4} \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & \frac{1-a_{3,2}}{a_{3,3}} & 0 & 0 \\ 0 & a_{3,2} & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,3}}{-1+a_{2,3}} & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{a_{3,3}}{-1+a_{2,3}} & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix},$$

$$\begin{pmatrix} -a_{1,3} & 1-a_{1,3}a_{2,4} & a_{1,3} & a_{1,3}a_{2,4} \\ 0 & -a_{2,4} & 1 & a_{2,4} \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \frac{1-a_{2,3}}{a_{3,3}} & a_{2,3} & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix},$$

$$\begin{pmatrix} \frac{(-1+a_{1,2}) a_{1,3}}{a_{1,2}} & a_{1,2} & a_{1,3} & 0 \\ 0 & -\frac{a_{1,2}}{a_{1,3}} & 0 & 0 \\ 0 & 0 & -\frac{a_{1,3}}{a_{1,2}} & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -a_{1,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & 0 & a_{1,3} & 0 \\ 0 & -\frac{a_{2,3}}{a_{1,3}} & a_{2,3} & 0 \\ 0 & 0 & \frac{a_{1,3}(-1+a_{2,3})}{a_{2,3}} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 1 & a_{1,3} & 1 \\ 0 & 0 & 1 & \frac{1}{a_{1,3}} \\ 0 & 0 & -a_{1,3} & 0 \\ 0 & 0 & 0 & -\frac{1}{a_{1,3}} \end{pmatrix}, \begin{pmatrix} -\frac{a_{1,3}}{a_{2,3}} & 0 & a_{1,3} & -\frac{a_{2,3}}{-1+a_{2,3}} \\ 0 & -\frac{a_{2,3}}{a_{1,3}} & a_{2,3} & -\frac{a_{2,3}^2}{a_{1,3}(-1+a_{2,3})} \\ 0 & 0 & \frac{a_{1,3}(-1+a_{2,3})}{a_{2,3}} & 0 \\ 0 & 0 & 0 & \frac{a_{2,3}}{a_{1,3}(-1+a_{2,3})} \end{pmatrix}, \begin{pmatrix} \frac{1}{2} \left(-a_{1,3} + \frac{\sqrt{a_{1,3}} \sqrt{4+a_{1,3} a_{2,4}}}{\sqrt{a_{2,4}}} \right) \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ a_{3,1} a_{4,2} & a_{4,2} & 1 & -a_{4,2} \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & \frac{-1+a_{4,3}}{a_{4,2}} & 0 \\ 0 & a_{4,2} & a_{4,3} & -a_{4,2} \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & a_{3,3} & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{2,4} \\ 0 & 0 & -\frac{1}{a_{2,4}} & 0 \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} \frac{2 a_{1,3}}{a_{1,3} a_{2,4} + \sqrt{a_{1,3}} \sqrt{a_{2,4}} \sqrt{4+a_{1,3} a_{2,4}}} & 0 \\ 0 & \frac{2 a_{2,4} + a_{1,3} a_{2,4}^2 + \sqrt{a_{1,3}} a_{2,4}^{3/2} \sqrt{4+a_{1,3} a_{2,4}}}{a_{1,3} a_{2,4} + \sqrt{a_{1,3}} \sqrt{a_{2,4}} \sqrt{4+a_{1,3} a_{2,4}}} \\ 0 & 0 \\ 0 & 0 \end{pmatrix}, \frac{1}{2} \left(-a_{1,3} a_2 \right), \underline{a_1},$$

$$\begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 0 & 0 & 1 & a_{2,4} \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} 0 & 1 & a_{1,3} & a_{1,3} a_{2,4} \\ 1 & 0 & 1 & a_{2,4} \\ 0 & 0 & -a_{1,3} & 1 - a_{1,3} a_{2,4} \\ 0 & 0 & 0 & -a_{2,4} \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 0 & -\frac{1}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 0 & -\frac{1}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ a_{3,1} & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} -a_{3,1} & 0 & 0 & 0 \\ 0 & -\frac{1}{a_{3,1}} & 0 & 0 \\ a_{3,1} & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix},$$

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & a_{2,2} & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

$$\begin{pmatrix} a_{1,1} & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} \frac{1}{a_{2,2}} & 0 & 0 & 0 \\ 0 & a_{2,2} & 0 & 0 \\ 0 & 0 & \frac{1}{a_{2,2}} & 0 \\ 0 & 0 & 0 & a_{2,2} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & a_{4,4} \end{pmatrix},$$

[illegible]

$$\begin{aligned}
& \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \\
& \left. \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \right\}
\end{aligned}$$